

Estimation of Electricity Production for a Moroccan Wind Farm

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Plan



Present the wind speed data

Model the wind speed distribution

Estimate the available wind power density

Estimate the usable wind power

Summary



Studied parks

Wind speed data

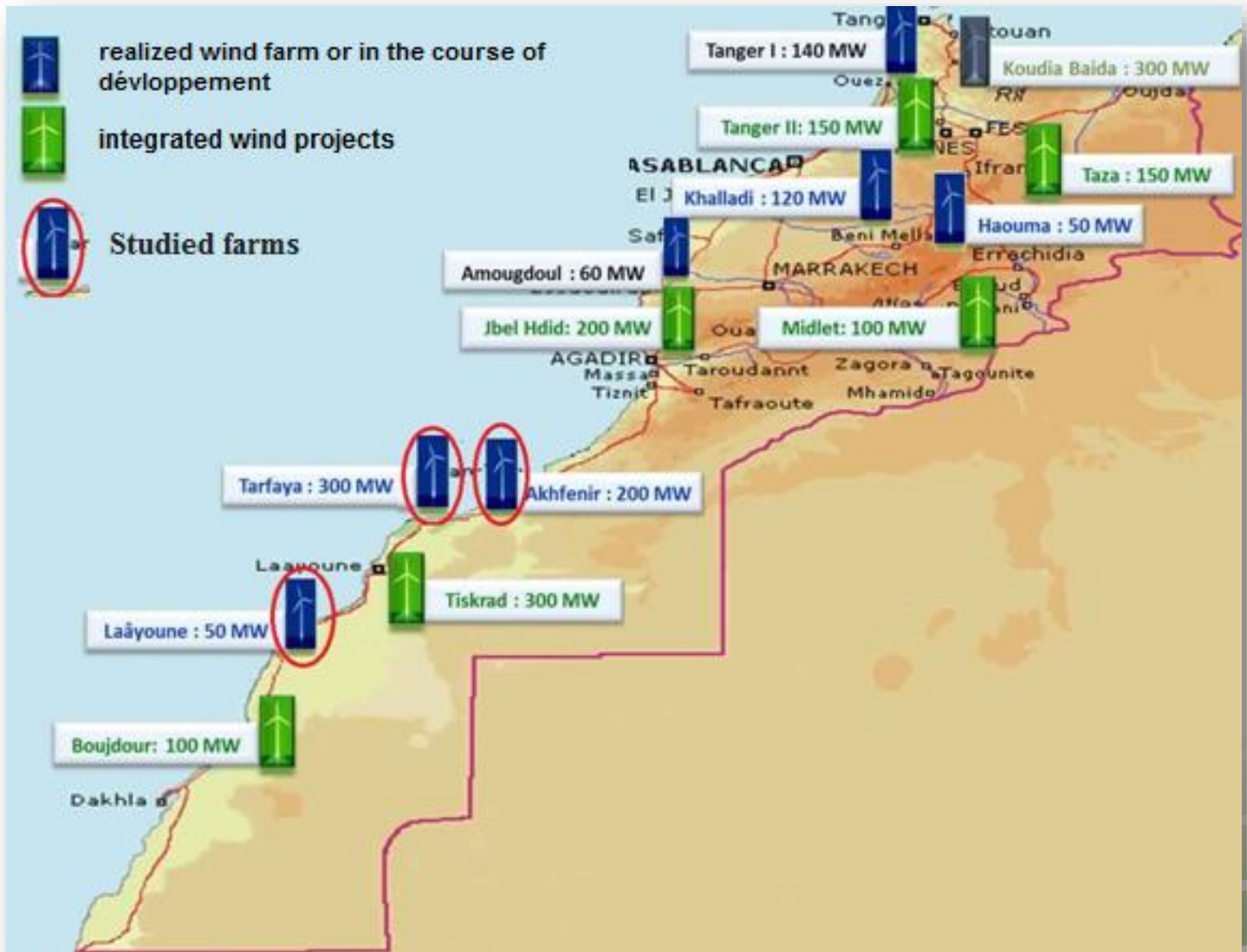
Wind speed data

Modeling the wind speed distribution

Estimation of available wind power density

Estimation of usable wind power

Summary

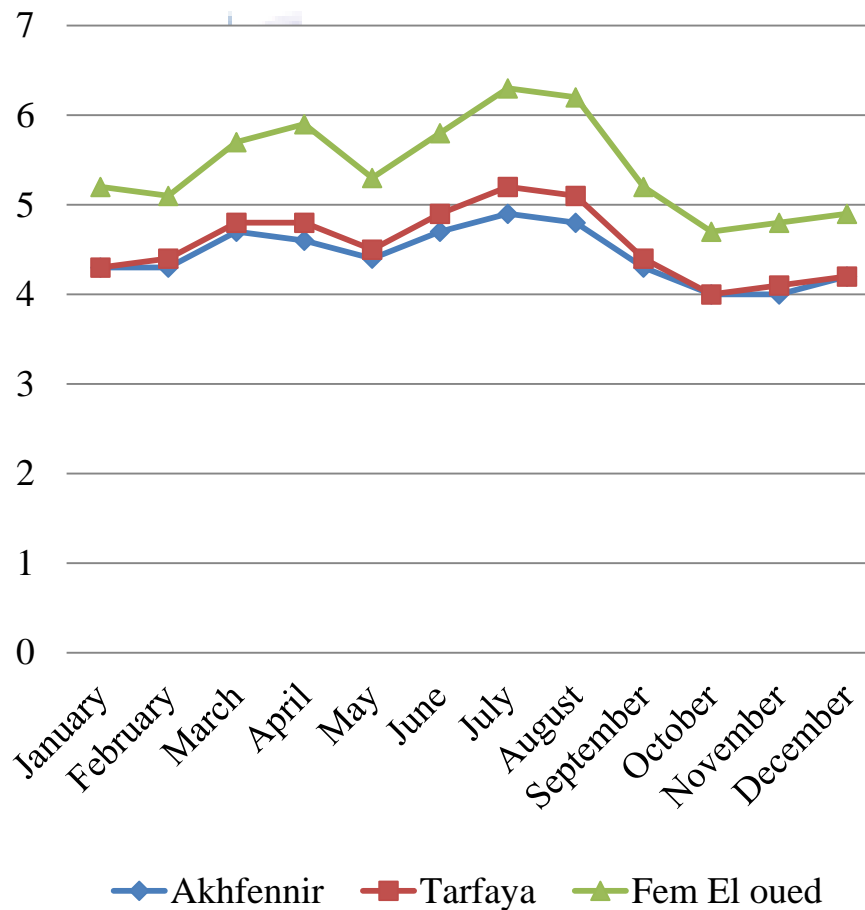


Studied parks

Wind speed data

Wind speed data

Wind speed (m/s)



| Month | Akhfennir | Tarfaya | Fem El Oued |
|-----------|-----------|---------|-------------|
| January | 4.3 | 4.3 | 5.2 |
| February | 4.3 | 4.4 | 5.1 |
| March | 4.7 | 4.8 | 5.7 |
| April | 4.6 | 4.8 | 5.9 |
| May | 4.4 | 4.5 | 5.3 |
| June | 4.7 | 4.9 | 5.8 |
| July | 4.9 | 5.2 | 6.3 |
| August | 4.8 | 5.1 | 6.2 |
| September | 4.3 | 4.4 | 5.2 |
| October | 4 | 4 | 4.7 |
| November | 4 | 4.1 | 4.8 |
| December | 4.2 | 4.2 | 4.9 |
| Average | 4.4 | 4.6 | 5.4 |

<https://eosweb.larc.nasa.gov/cgi-bin/sse/sse.cgi?rets@nrcan.gc.ca>

Wind speed modelisation

Estimation of Weibull parameters at 10 m

Extrapolation of Weibull parameters at 80 m

Wind speed
data



- Weibull
- Rayleigh
- Lognormal ...

Modeling the
wind speed
distribution

Estimation of
Available wind
power density

- ✓ **Weibull** is widely used, accepted and recommended in the literature.
- ✓ it gives a good agreement with the experimental data.
- ✓ it allows determining quickly the average production of a wind turbine.

Estimation of
Usable wind
power

Summary

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Extrapolation of Weibull parameters at 80 m

$$f(v) = \left(\frac{k}{c}\right) \left(\frac{v}{c}\right)^{k-1} \exp\left(-\left(\frac{v}{c}\right)^k\right)$$

- v : the wind speed (m/s)
- k : shape factor
- c : scale factor (m/s)

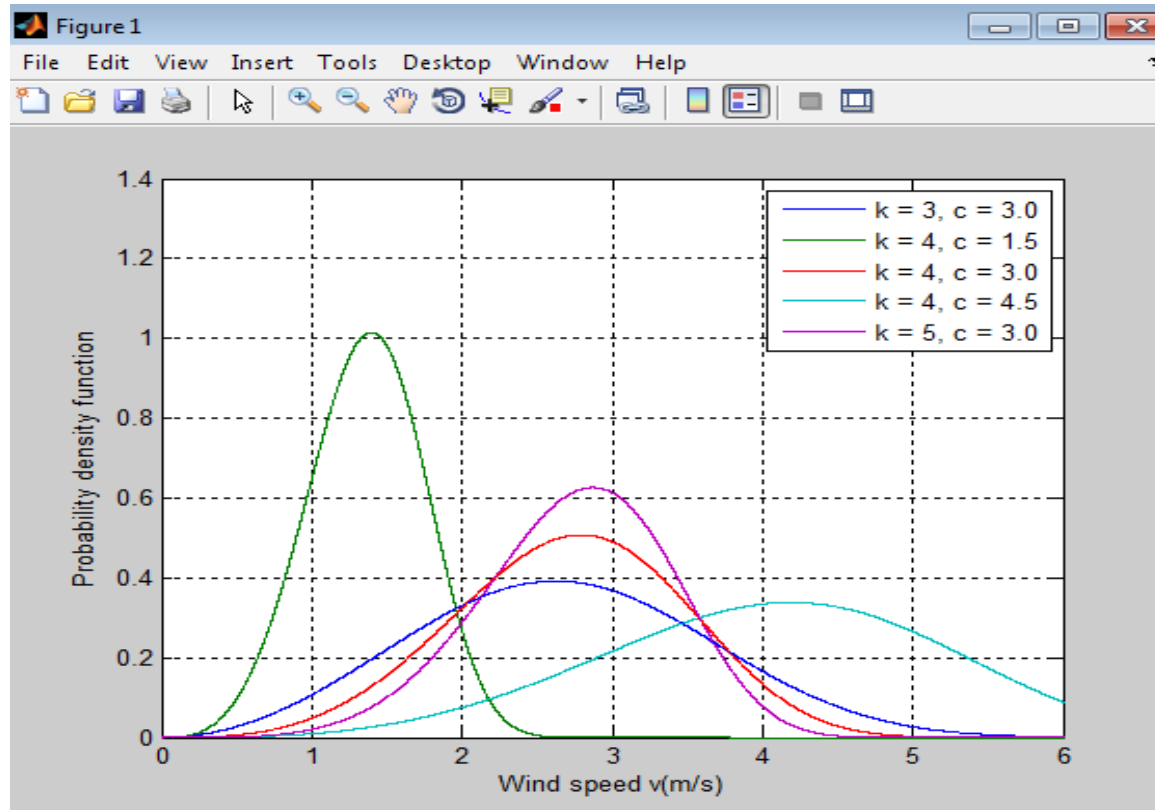
Wind speed data

Modeling the wind speed distribution

Estimation of Available wind power density

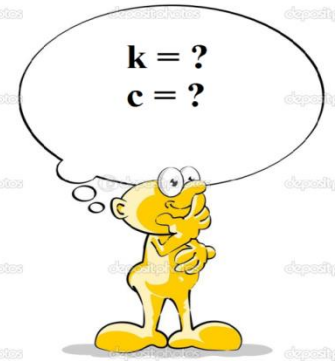
Estimation of Usable wind power

Summary



Wind speed
data

➤ The method proposed by
Mabchour in 1999.



$$k = 1 + (0.483 * (\bar{v} - 2))^{0.51}$$



Arithmetic mean
of wind speed

$$c = \frac{\bar{v}}{\Gamma\left(1 + \frac{1}{k}\right)}$$



Gamma function

Modeling the
wind speed
distribution

Estimation of
Available wind
power density

Estimation of
Usable wind
power

Summary

Wind speed modelisation

Estimation of Weibull parameters at 10 m

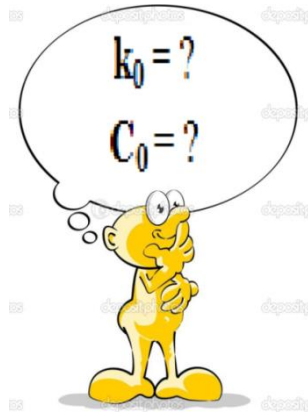
Extrapolation of Weibull parameters at 80 m

- Wind speed data
- Modeling the wind speed distribution
- Estimation of Available wind power
- Estimation of Usable wind power
- Summary

| Month | Akhfennir | | Tarfaya | | Fem El Oued | |
|-----------|-------------|-------|-------------|-------|-------------|-------|
| | C_0 (m/s) | k_0 | C_0 (m/s) | k_0 | C_0 (m/s) | k_0 |
| January | 4.85 | 2.06 | 4.86 | 2.06 | 5.87 | 2.25 |
| February | 4.85 | 2.06 | 4.97 | 2.08 | 5.76 | 2.23 |
| March | 5.31 | 2.15 | 5.42 | 2.17 | 6.43 | 2.34 |
| April | 5.19 | 2.12 | 5.42 | 2.17 | 6.66 | 2.38 |
| May | 4.97 | 2.08 | 5.08 | 2.1 | 5.98 | 2.27 |
| June | 5.31 | 2.15 | 5.53 | 2.19 | 6.55 | 2.36 |
| July | 5.53 | 2.19 | 5.87 | 2.25 | 7.11 | 2.45 |
| August | 5.42 | 2.17 | 5.76 | 2.23 | 7 | 2.43 |
| September | 4.85 | 2.06 | 4.97 | 2.08 | 5.87 | 2.25 |
| October | 4.52 | 1.98 | 4.52 | 1.98 | 5.31 | 2.15 |
| November | 4.52 | 1.98 | 4.63 | 2.01 | 5.42 | 2.17 |
| December | 4.74 | 2.03 | 4.74 | 2.03 | 5.53 | 2.19 |
| Average | 5.00 | 2.08 | 5.15 | 2.11 | 6.12 | 2.29 |

Fem El Oued is the **windiest** farm.

wind speed is more **uniform** in Fem El Oued



Wind speed
data

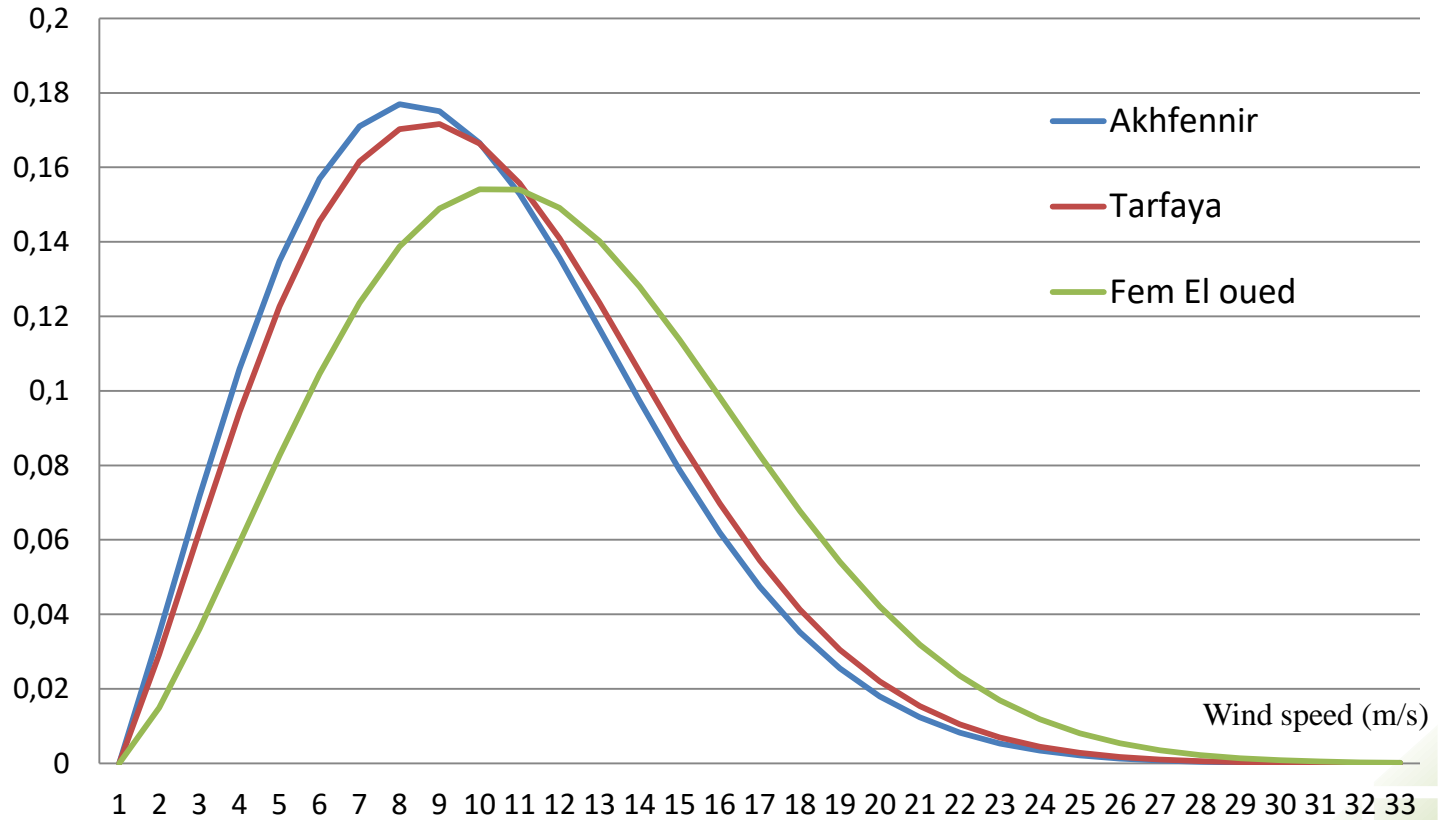
Modeling the
wind speed
distribution

Estimation of
Available wind
power density

Estimation of
Usable wind
power

Summary

Adjustment of the Weibull law on the wind speed distribution of the three parks at height of 10 m.



Wind speed
data

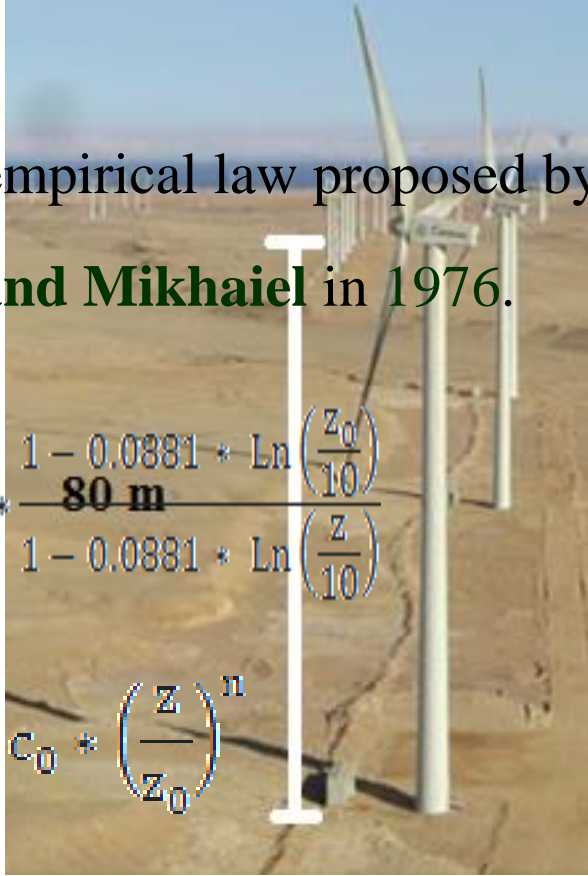
Modeling the
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Estimation of
Available wind
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Estimation of
Usable wind
power

Summary

➤ The empirical law proposed by
Justus and Mikhael in 1976.


$$k_z = k_0 * \frac{1 - 0.0881 * \ln\left(\frac{z_0}{10}\right)}{80 \text{ m} * \left(1 - 0.0881 * \ln\left(\frac{z}{10}\right)\right)}$$

$$c_z = c_0 * \left(\frac{z}{z_0}\right)^n$$

$$n = \frac{0.37 - 0.0881 * \ln c_0}{1 - 0.0881 * \ln\left(\frac{z_0}{10}\right)}$$

Wind speed modelisation

Estimation of Weibull parameters at 10 m

Extrapolation of Weibull parameters at 80 m

- Wind speed data
- Modeling the wind speed distribution
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- Estimation of Usable wind power
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| Month | Akhfennir | | Tarfaya | | Fem El Oued | |
|-----------|----------------|----------|----------------|----------|----------------|----------|
| | C_{80} (m/s) | k_{80} | C_{80} (m/s) | k_{80} | C_{80} (m/s) | k_{80} |
| January | 7.84 | 2.52 | 7.85 | 2.52 | 9.16 | 2.75 |
| February | 7.84 | 2.52 | 7.99 | 2.54 | 9.02 | 2.73 |
| March | 8.44 | 2.63 | 8.58 | 2.65 | 9.87 | 2.87 |
| April | 8.29 | 2.6 | 8.58 | 2.65 | 10.16 | 2.92 |
| May | 7.99 | 2.54 | 8.14 | 2.57 | 9.3 | 2.78 |
| June | 8.44 | 2.63 | 8.73 | 2.68 | 10.02 | 2.89 |
| July | 8.73 | 2.68 | 9.16 | 2.75 | 10.72 | 3 |
| August | 8.58 | 2.65 | 9.02 | 2.73 | 10.58 | 2.98 |
| September | 7.84 | 2.52 | 7.99 | 2.54 | 9.16 | 2.75 |
| October | 7.39 | 2.43 | 7.4 | 2.43 | 8.44 | 2.63 |
| November | 7.39 | 2.43 | 7.55 | 2.46 | 8.58 | 2.65 |
| December | 7.7 | 2.49 | 7.7 | 2.49 | 8.73 | 2.68 |

Available wind power density

Estimated Available wind power density

The average of available wind power density is given by:

$$P_{av} = \frac{1}{2} \rho v^3$$

Air density in (kg/m³)

$$\langle v^3 \rangle = c^3 \cdot \Gamma\left(1 + \frac{3}{k}\right)$$

$$\rho = 3.485 \frac{P}{T}$$

$\frac{P}{T}$ —————> Pression en (k Pa)
 $\frac{P}{T}$ —————> Temperature (k)

| | Akhfennir | Tarfaya | Fem El Oued |
|--|-------------|-------------|-------------|
| P: Pressure average (kPa) | 99 | 100 | 101 |
| T: Temperature average (K) | 294.45 | 294.55 | 293.15 |
| ρ: Air density average (kg/m³) | 1.17 | 1.18 | 1.20 |

Wind speed data

Modeling the wind speed distribution

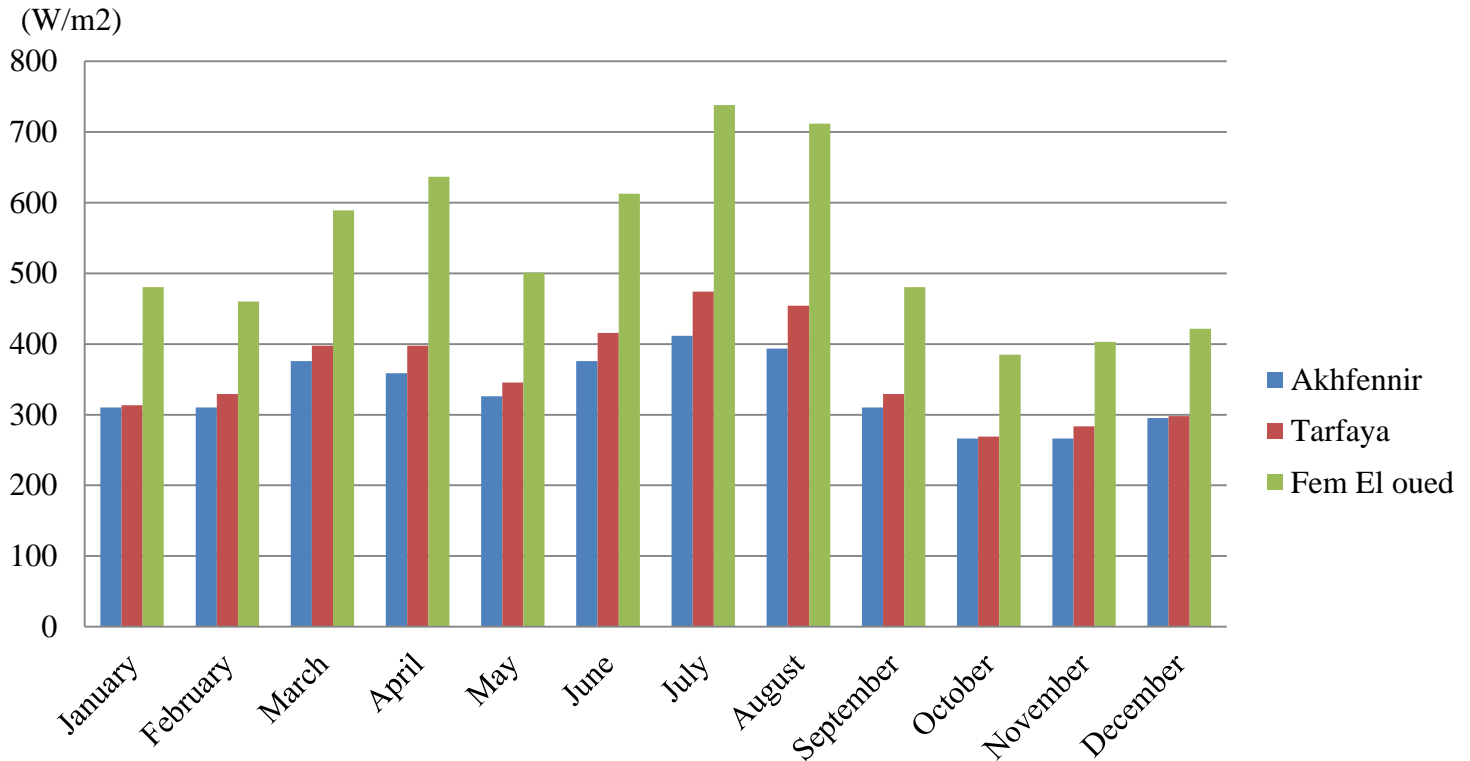
Estimation of Available wind power density

Estimation of Usable wind power

Summary

Available wind power density

Estimated available wind power density



The investment in Fem El Oued can be profitable

Wind speed data

Modeling the wind speed distribution

Estimation of Available wind power density

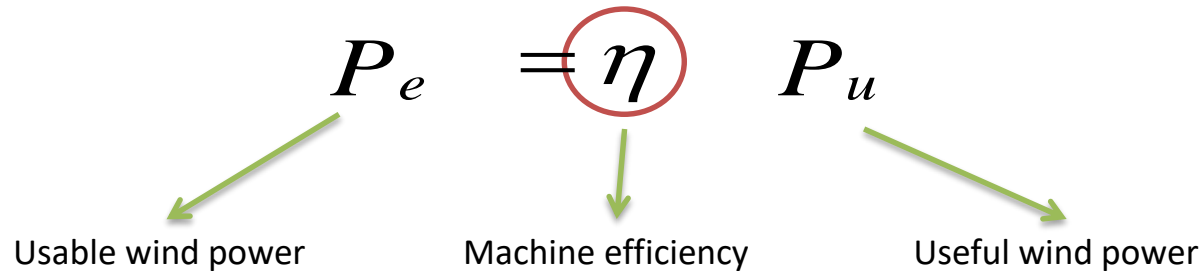
Estimation of Usable wind power

Summary

Machine efficiency

Useful wind power

Usable wind power



$$\eta = 2 \times \frac{P_r}{\rho A v_r^3}$$

P_r : rated power

A: swept area

v_r : rated wind speed

| | | P_r per unit (KW) | A (m ²) | V_r (m/s) | Efficiency (%) |
|-------------|---------|---------------------|---------------------|-------------|----------------|
| Akhfennir | Field 1 | 1670 | 11700 | 11 | 11.09 |
| | Field 2 | 1700 | 7854 | 13 | 27.76 |
| Tarfaya | | 2300 | 8012 | 12 | 28.08 |
| Fem EL oued | | 2300 | 8012 | 12 | 28.08 |

Wind speed data

Modeling the wind speed distribution

Estimation of Available wind power density

Estimation of Usable wind power

Summary

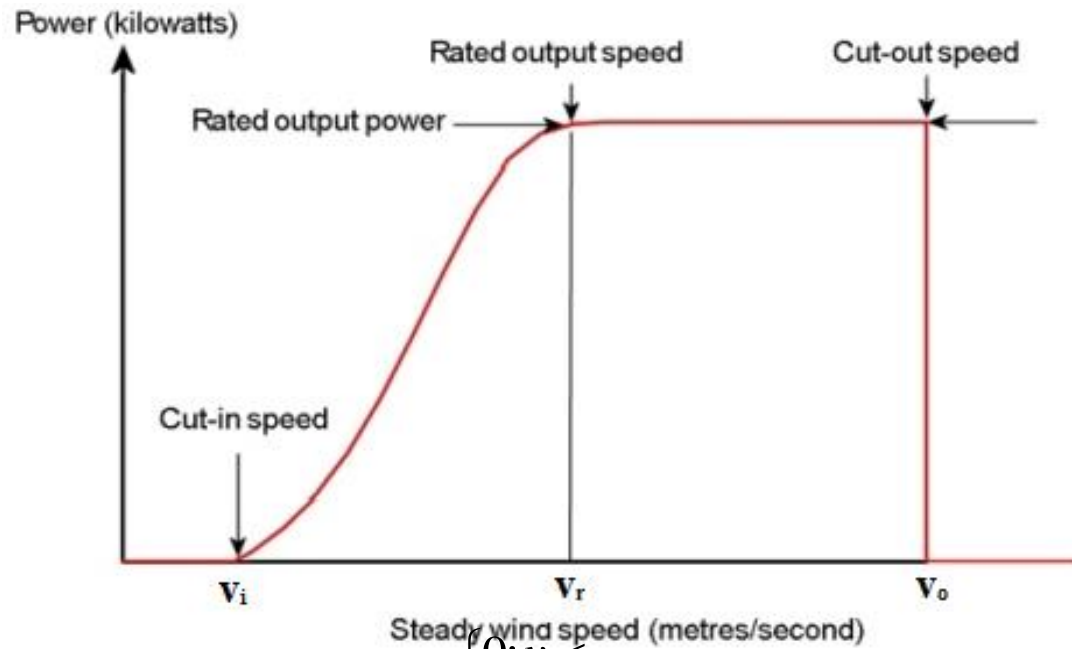
Wind speed data

Modeling the wind speed distribution

Estimation of Available wind power density

Estimation of Usable wind power

Summary



$$P_u = \begin{cases} 0; & v < v_i \\ \frac{1}{2} \rho v^3 & ; v_i \leq v \leq v_r \\ \frac{1}{2} \rho v_r^3 & ; v_r \leq v \leq v_o \\ 0; & v \geq v_o \end{cases}$$

Machine efficiency

Useful wind power

Usable wind power

| | | Turbines manufacturer | Turbines model | Number of turbine | Cut-in speed (m/s) | Rated speed (m/s) | Cut-out speed (m/s) |
|-------------|---------|-----------------------|----------------|-------------------|--------------------|-------------------|---------------------|
| Akhfennir | Field 1 | General Electric | 1.7-100 | 61 | 3.5 | 11 | 23 |
| | Field 2 | Alstom- Ecotècnia | ECO 74 | 56 | 3 | 13 | 25 |
| Tarfaya | | Siemens SWT-2.3-101 | SWT-2.3-101 | 131 | 3 | 12 | 20 |
| Fem El oued | | Siemens SWT-2.3-101 | SWT-2.3-101 | 22 | 3 | 12 | 20 |

<http://eolienne.f4jr.org/>



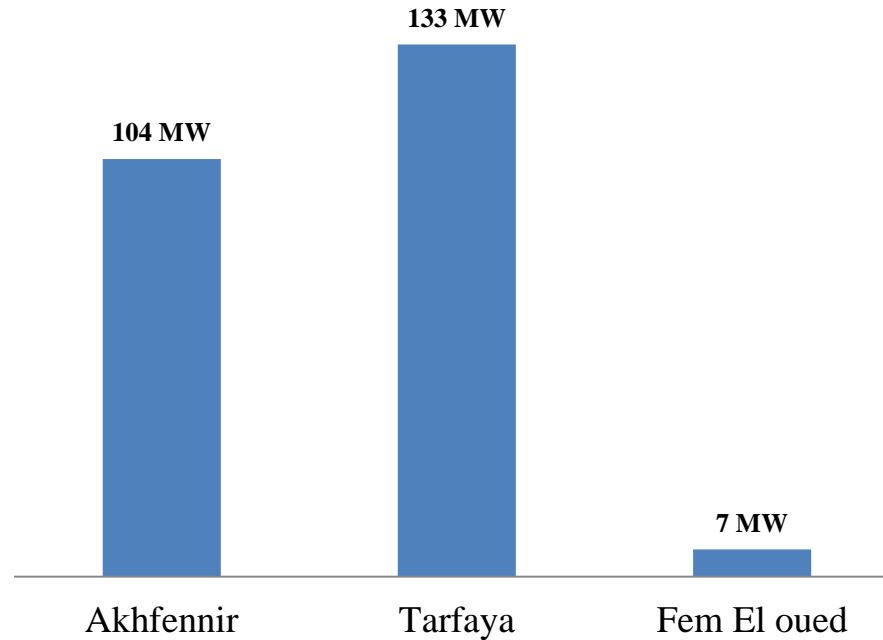
The estimated useful power is **537 MW** in Akhfennir, **473 MW** in Tarfaya and **25 MW** in Fem El oued.

Machine efficiency

Useful wind power

Usable wind power

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This result depends not only on the available power at each park, but also on the number of wind turbines and their characteristics, that is why Fem El Oued has the lowest production.

Summary

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data

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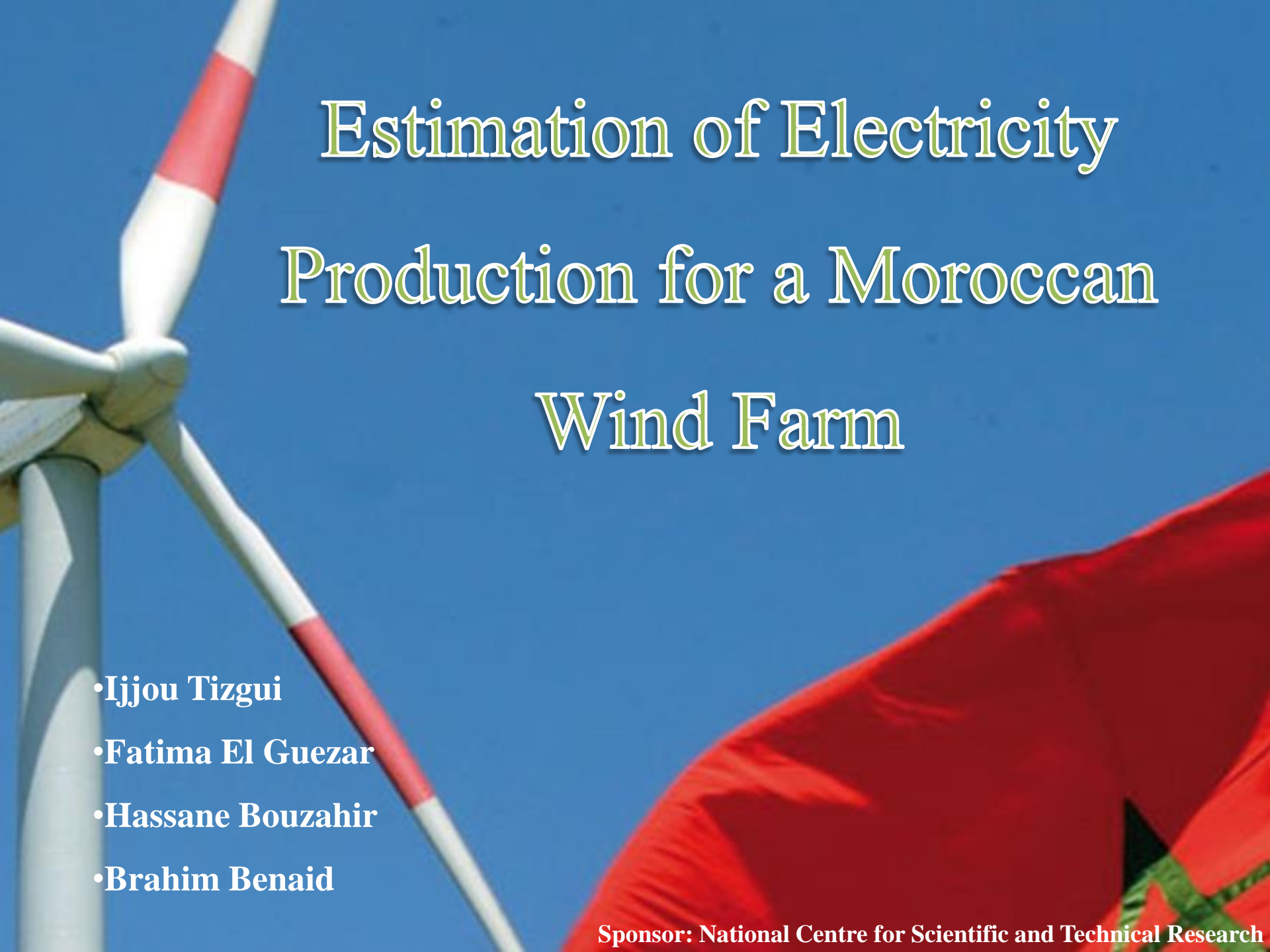
Estimation of
Usable wind
power

Summary

- ✓ Fem El Oued is the windiest park, and the wind speed is more uniform in this park.
- ✓ The wind potential is very important in Fem El Oued, so, the investment in this park can be profitable.
- ✓ Fem El Oued has the lowest production because there is a less number of turbines.



Thank You



Estimation of Electricity Production for a Moroccan Wind Farm

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